# A Simple Class-AB Transconductor in CMOS

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May 19, 2008



# Simple EKV MOS Transistor Model

We model the channel current of an nMOS transistor as the difference between a forward current and a reverse current,

$$I = I_{\rm F} - I_{\rm R},$$

whose values are given by

$$I_{\rm F(R)} = SI_{\rm s} \log^2 \left( 1 + e^{\left(\kappa (V_{\rm G} - V_{\rm T0}) - V_{\rm S(D)}\right)/2U_{\rm T}} \right),$$

where

$$U_{\rm T} = \frac{kT}{q}, \quad S = \frac{W}{L}, \quad I_{\rm s} = \frac{2\mu C_{\rm ox} U_{\rm T}^2}{\kappa}, \quad \text{and} \quad \kappa = \frac{C_{\rm ox}}{C_{\rm ox} + C_{\rm dep}}.$$

Note that  $SI_s$  is approximately twice the saturation current at threshold. This simple model covers all regions of normal MOS transistor operation.



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 $V_{\rm G} \longrightarrow S$ 

### Simple EKV MOS Transistor Model

The expressions for  $I_{\rm F}$  and  $I_{\rm R}$  reduce asymptotically to an exponential form in weak inversion and a quadratic form in strong inversion, given by

$$I_{\rm F(R)} \approx \begin{cases} SI_{\rm s}e^{\left(\kappa(V_{\rm G}-V_{\rm T0})-V_{\rm S(D)}\right)/U_{\rm T}}, & I_{\rm sat} \\ V_{\rm G} < V_{\rm T0} + \frac{V_{\rm S(D)}}{\kappa} \\ \frac{SI_{\rm s}}{4U_{\rm T}^2} \left(\kappa\left(V_{\rm G}-V_{\rm T0}\right)-V_{\rm S(D)}\right)^2, & I_{\rm sat} \\ V_{\rm G} > V_{\rm T0} + \frac{V_{\rm S(D)}}{\kappa}. & I_{\rm sat} \\ V_{\rm G} > V_{\rm T0} + \frac{V_{\rm S(D)}}{\kappa}. & I_{\rm sat} \\ V_{\rm G} > V_{\rm T0} + \frac{V_{\rm S(D)}}{\kappa}. & I_{\rm sat} \\ I_{\rm sat} > I_{\rm sat} > I_{\rm sat} \\ I_{\rm sat} > I_{\rm sat} > I_{\rm sat} \\ I_{\rm sat} > I_{\rm sat} > I_{\rm sat} \\ I_{\rm sat} > I_{\rm sat} > I_{\rm sat} > I_{\rm sat} \\ I_{\rm sat} > I_$$







## Simple EKV MOS Transistor Model

The expressions for  $I_{\rm F}$  and  $I_{\rm R}$  are also explicitly invertible; the inverses are given by

$$\kappa \left( V_{\rm G} - V_{\rm T0} \right) - V_{\rm S(D)} = 2U_{\rm T} \log \left( e^{\sqrt{I_{\rm F(R)}/SI_{\rm s}}} - 1 \right)$$

$$\approx \begin{cases} U_{\rm T} \log \frac{I_{\rm F(R)}}{SI_{\rm s}}, & I_{\rm F(R)} \ll SI_{\rm s} \\ 2U_{\rm T} \sqrt{\frac{I_{\rm F(R)}}{SI_{\rm s}}}, & I_{\rm F(R)} \gg SI_{\rm s}. \end{cases}$$





### Delbrück's Bump/Antibump Circuit

If the bias current,  $I_{\rm b}$ , is in weak inversion, then the bump current,  $I_3$ , is an even-symmetric, bell-shaped function of the differential-mode input voltage,  $V_{\rm dm} = V_1 - V_2$ , given by

$$I_3 = \frac{I_{\rm b}}{2} \operatorname{sech}^2 \left( \frac{\kappa V_{\rm dm}}{2U_{\rm T}} \right).$$

Note that the three output currents sum to a constant,  $I_{\rm b}$ , so the sum  $I_1 + I_2$  is just  $I_{\rm b}$  less the bump current, which is the antibump current.





#### A Variation of the Bump/Antibump Circuit

Now, suppose that we fix the bump current to be a constant,  $I_{\rm b}$ . If  $I_1$ ,  $I_2$ , and  $I_{\rm b}$  are in weak inversion, we have that

$$I_1 = SI_{\rm s} e^{(\kappa(V_1 - V_{\rm T0}) - V)/U_{\rm T}},$$

$$I_2 = SI_{\rm s}e^{(\kappa(V_2 - V_{\rm T0}) - V)/U_{\rm T}},$$

and

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$$I_{\rm b} = \frac{I_1 I_2}{I_1 + I_2} = I_1 \| I_2.$$





## A Variation of the Bump/Antibump Circuit

Now, consider the quantity

$$I_{\rm b} = I_1 || I_2$$
  
=  $SI_{\rm s} e^{(\kappa(V_1 - V_{\rm T0}) - V)/U_{\rm T}} || SI_{\rm s} e^{(\kappa(V_2 - V_{\rm T0}) - V)/U_{\rm T}}$   
=  $SI_{\rm s} e^{-\kappa V_{\rm T0}/U_{\rm T}} e^{-V/U_{\rm T}} \left( e^{\kappa V_1/U_{\rm T}} || e^{\kappa V_2/U_{\rm T}} \right),$ 

which implies that

$$SI_{s}e^{-\kappa V_{T0}/U_{T}}e^{-V/U_{T}} = \frac{I_{b}}{e^{\kappa V_{1}/U_{T}} ||e^{\kappa V_{2}/U_{T}}}.$$





### A Variation of the Bump/Antibump Circuit

By substituting this result back into the equations for  $I_1$  and  $I_2$ , we find that

$$I_{1} = \frac{I_{\rm b} e^{\kappa V_{1}/U_{\rm T}}}{e^{\kappa V_{1}/U_{\rm T}} \| e^{\kappa V_{2}/U_{\rm T}}} = I_{\rm b} \left( 1 + e^{\kappa (V_{1} - V_{2})/U_{\rm T}} \right) = I_{\rm b} \left( 1 + e^{\kappa V_{\rm dm}/U_{\rm T}} \right),$$

that

$$I_{2} = \frac{I_{\rm b} e^{\kappa V_{2}/U_{\rm T}}}{e^{\kappa V_{1}/U_{\rm T}} \|e^{\kappa V_{2}/U_{\rm T}}} = I_{\rm b} \left(1 + e^{-\kappa (V_{1} - V_{2})/U_{\rm T}}\right) = I_{\rm b} \left(1 + e^{-\kappa V_{\rm dm}/U_{\rm T}}\right),$$

and that

$$I_1 - I_2 = I_{\rm b} \left( e^{\kappa V_{\rm dm}/U_{\rm T}} - e^{-\kappa V_{\rm dm}/U_{\rm T}} \right) = 2I_{\rm b} \sinh\left(\frac{\kappa V_{\rm dm}}{U_{\rm T}}\right)$$





#### Fixing the Bump Current at $I_{\rm b}$









**Bias Circuit for Folded-Cascode/Flipped-Follower** 





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#### Analytical Model of Output Current versus $V_{dm}$

By using the simplified EKV model of the MOS transistor, we can show that

$$I_{1} = I_{\rm b} + SI_{\rm s} \log^{2} \left( 1 + e^{\kappa V_{\rm dm}/2U_{\rm T}} \left( e^{\sqrt{I_{\rm b}/SI_{\rm s}}} - 1 \right) \right)$$

and that

$$I_2 = SI_{\rm s} \log^2 \left( 1 + e^{-\kappa V_{\rm dm}/2U_{\rm T}} \left( e^{\sqrt{I_1/SI_{\rm s}}} - 1 \right) \right),$$

where all the symbols have their previously defined meanings.

Note that the model equation for  $I_2$  is expressed in terms of  $I_1$ , which, in turn, is an explicit function of  $V_{dm}$ . So, we can obtain explicit expressions for  $I_2$  and  $I_1 - I_2$  in terms of  $V_{dm}$ , but it is unclear that doing so is of much value, because doing so leads to *very* cumbersome expressions.





## Output Currents versus $V_{dm}$







## Differential Output Current versus $V_{dm}$







### Differential-Mode Transconductance versus $V_{\rm cm}$





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# **Enhanced-Slew-Rate Folded-Cascode Amplifier**







Enhanced-Slew-Rate Folded-Cascode Amplifier Step Response





